

Who Will (Most Likely) Win the 2018 FIFA World Cup?

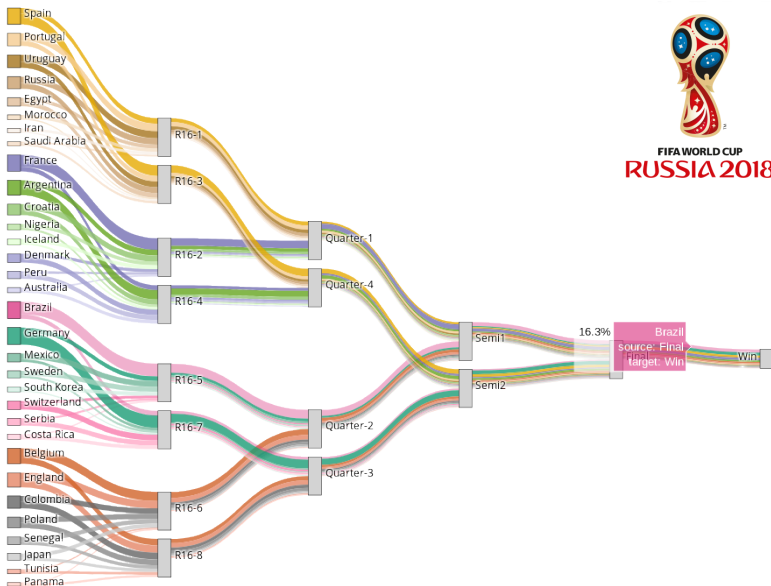
Achim Zeileis

<https://eeecon.uibk.ac.at/~zeileis/>

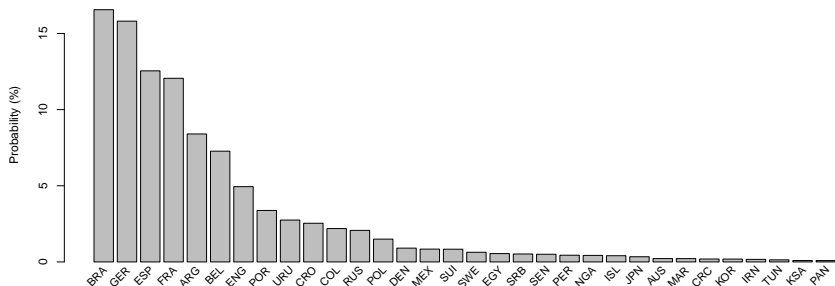
2018 FIFA World Cup prediction



FIFA WORLD CUP
RUSSIA 2018

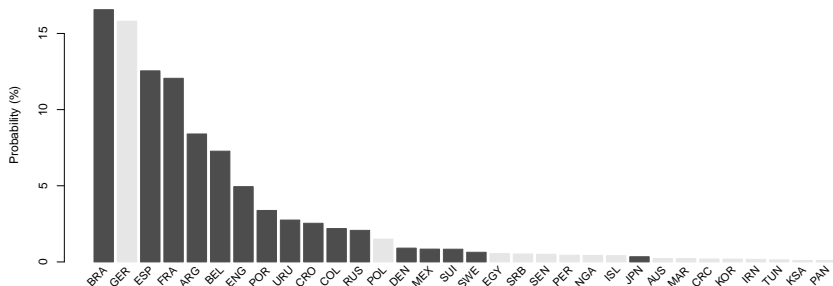


2018 FIFA World Cup prediction



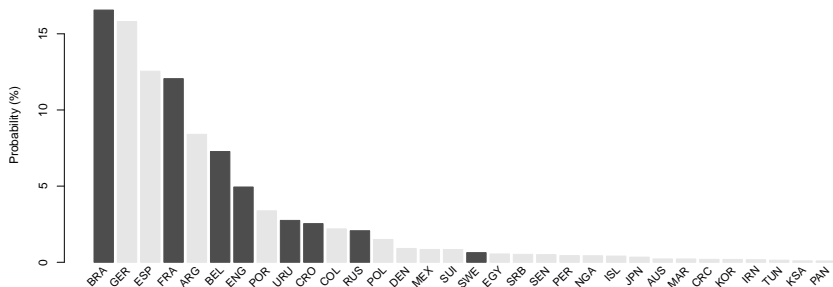
- Tournament forecast based on bookmakers odds.
- Main results: Brazil and Germany are the top favorites with winning probabilities of 16.6% and 15.8%.
- Brazil most likely plays France in the first semifinal (8.4%) and Germany Spain in the second (8%).

2018 FIFA World Cup prediction



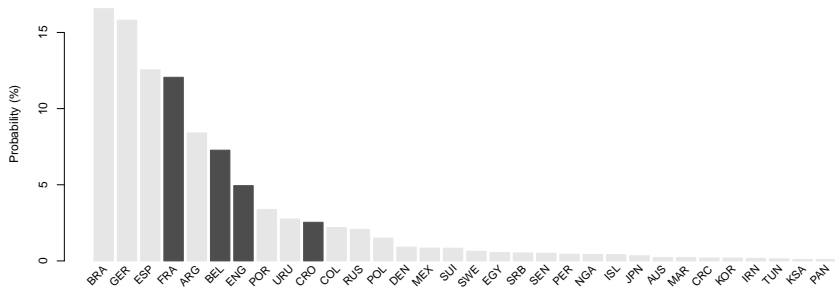
- Defending champion Germany surprisingly loses two matches, comes in last in its group, and drops out.
- All other favorites “survive” the group stage.
- Poland is also eliminated and instead Japan proceeds to the round of 16.

2018 FIFA World Cup prediction



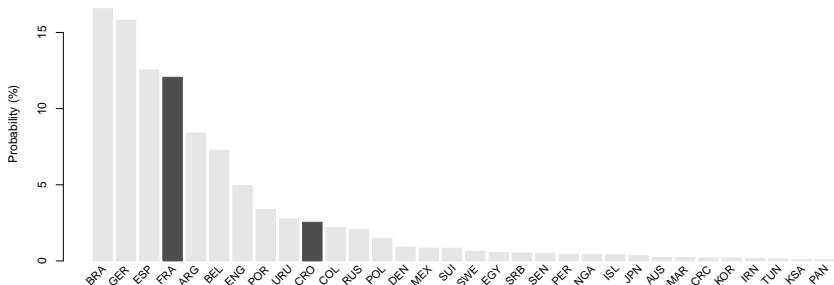
- France beats Argentina 4:3.
- Spain is eliminated by host Russia in penalties.
- Belgium turns a 0:2 into a 3:2 against Japan.
- Uruguay (with Cavani) beats European champion Portugal.

2018 FIFA World Cup prediction



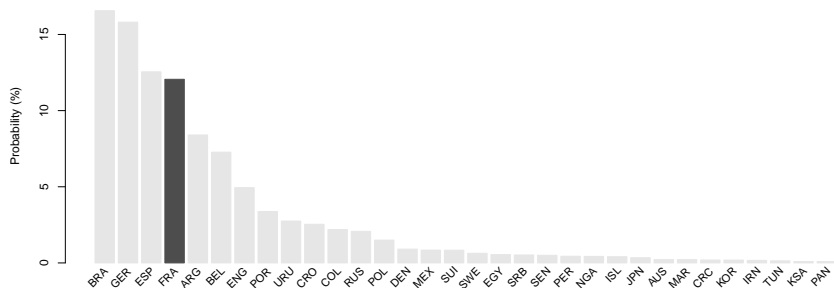
- France beats Uruguay (without Cavani) 2:0.
- Brazil loses in a great and close game to Belgium.
- England clearly beats Sweden.
- Croatia eliminates host Russia in penalties.

2018 FIFA World Cup prediction



- France cleverly beats Belgium 1:0 with a set-piece goal and a controlled game.
- After trailing 0:1 against England, Croatia turns the game in the second half and the decisive goal in extra time.

2018 FIFA World Cup prediction



- France wins the final in another clever team effort 4:2.

Bookmakers odds

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You are here: [Football](#) > [All Competitions](#) > [World Cup 2018](#) > [Outright](#) | Price Format: | Bet until: 04 Sep -12:00 UK

World Cup 2018 - Outright - All Markets

▼ Tournament Winner 17

Germany	6.50	Argentina	8.00	France	9.00
Brazil	10.00	Spain			
England	17.00	Holland			
Chile	21.00	Russia			
Colombia	34.00	Croatia			

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Football Betting Odds

Bet types

☒ Outright winner (1)

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★ **World Cup 2018 - World**

Outright winner

Sunday - 7/8/2018

World Cup 2018 - Winner 8:00 PM

Tournament winner

★ Germany	6.00	★ France	8.00
★ Argentina	10.00	★ Spain	10.00
★ Brazil	11.00	★ Italy	13.00

Bookmakers odds: Motivation

Forecasts of sports events:

- Increasing interest in forecasting of competitive sports events due to growing popularity of online sports betting.
- Forecasts often based on ratings or rankings of competitors' ability/strength.

In football:

- Elo rating.
 - Aims to capture relative strength of competitors yielding probabilities for pairwise comparisons.
 - Originally developed for chess.
- FIFA rating.
 - Official ranking, used for seeding tournaments.
 - Often criticized for not capturing *current* strengths well.
 - June 2018: Decision to change calculation to be more similar to Elo.

Bookmakers odds: Motivation

Alternatively: Employ bookmakers odds for winning a competition.

- Bookmakers are “experts” with monetary incentives to rate competitors correctly. Setting odds too high or too low yields less profits.
- Prospective in nature: Bookmakers factor not only the competitors abilities into their odds but also tournament draws/seedings, home advantages, recent events such as injuries, etc.
- Statistical “post-processing” needed to derive winning probabilities and underlying abilities.

Bookmakers odds: Statistics

Odds: In statistics, the ratio of the probabilities for/against a certain event,

$$odds = \frac{p}{1 - p}.$$

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Illustrations:

- Even odds are “50:50” ($= 1$).
- Odds of 4 correspond to probabilities $4/5 = 80\%$ vs. $1/5 = 20\%$.

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Thus: Odds can be converted to probabilities and vice versa.

$$p = \frac{odds}{odds + 1}$$
$$1 - p = \frac{1}{odds + 1}$$

Bookmakers odds: Quoted odds

Quoted odds: In sports betting, the payout for a stake of 1.

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Thus: “Naive” computation of probability

$$p = \frac{1}{\text{quoted odds}}.$$

Bookmakers odds: Quoted odds

Illustration: Quoted odds for bwin obtained on 2018-05-20.

Team	Quoted odds	"Naive" probability
Brazil	5.0	0.200
Germany	5.5	0.182
Spain	7.0	0.143
France	7.5	0.133
	⋮	
Saudi Arabia	501.0	0.002
Panama	1001.0	0.001

Bookmakers odds: Quoted odds

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Problem: Probabilities of all 32 teams sum to $1.143 > 1$.

Bookmakers odds: Adjustment

Reason: Bookmakers do not give honest judgment of winning chances but include a profit margin known as “overround”.

Simple solution: Adjust quoted odds by factor 1.143 so that probabilities sum to 1.

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Team	Adjusted odds	Probability
Brazil	5.71	0.175
Germany	6.28	0.159
Spain	8.00	0.125
France	8.57	0.117
	⋮	

Bookmakers odds: Overround

Refinement: Apply adjustment only to the odds, not the stake.

$$\textit{quoted odds}_i = \textit{odds}_i \cdot \delta + 1,$$

- where \textit{odds}_i is the bookmaker's "true" judgment of the odds for competitor i ,
- δ is the bookmaker's payout proportion (overround: $1 - \delta$),
- and $+1$ is the stake.

Bookmakers odds: Overround

Winning probabilities: The adjusted $odds_i$ then corresponding to the odds of competitor i for losing the tournament. They can be easily transformed to the corresponding winning probability

$$p_i = \frac{1}{odds_i + 1}.$$

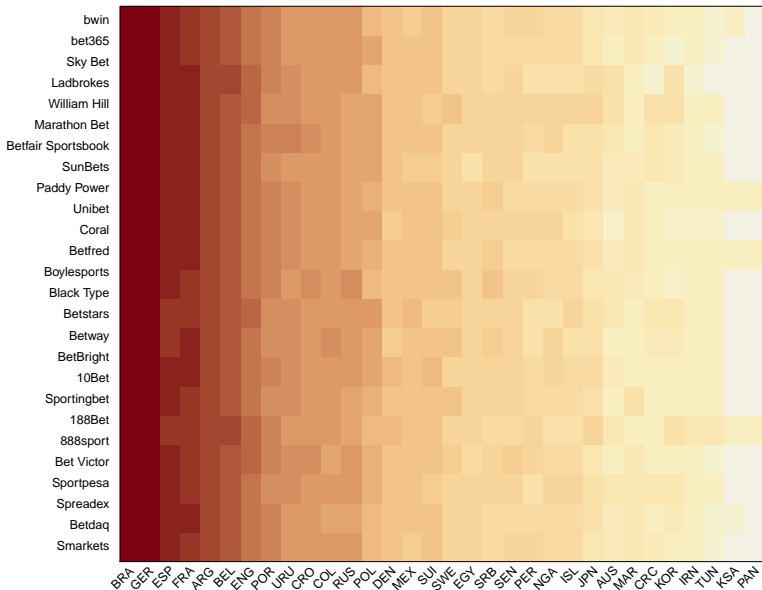
Determining the overround: Assuming that a bookmaker's overround is constant across competitors, it can be determined by requiring that the winning probabilities of all competitors (here: all 32 teams) sum to 1: $\sum_i p_i = 1$.

Bookmakers odds: 2018 FIFA World Cup

Data processing:

- Quoted odds from 26 online bookmakers.
- Obtained on 2018-05-20 from <http://www.bwin.com/> and <http://www.oddschecker.com/>.
- Computed overrounds $1 - \delta_b$ individually for each bookmaker $b = 1, \dots, 26$ by unity sum restriction across teams $i = 1, \dots, 32$.
- Median overround is 15.2%.
- Yields overround-adjusted and transformed winning probabilities $p_{i,b}$ for each team i and bookmaker b .

Modeling consensus and agreement



Modeling consensus and agreement

Goal: Get consensus probabilities by aggregation across bookmakers.

Straightforward: Compute average for team i across bookmakers.

$$\bar{p}_i = \frac{1}{26} \sum_{b=1}^{26} p_{i,b}.$$

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Refinements:

- Statistical model assuming for latent consensus probability p_i for team i along with deviations $\varepsilon_{i,b}$.
- Additive model is plausible on suitable scale, e.g.,

$$\text{logit}(p) = \log \left(\frac{p}{1-p} \right).$$

Modeling consensus and agreement

Model: Bookmaker consensus model

$$\text{logit}(p_{i,b}) = \text{logit}(p_i) + \varepsilon_{i,b},$$

where further effects could be included, e.g., group effects in consensus logits or bookmaker-specific bias and variance in $\varepsilon_{i,b}$.

Modeling consensus and agreement

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Analogously: Methodology can also be used for consensus ratings of default probability in credit risk rating of bank b for firm i .

Modeling consensus and agreement

Here:

- Simple fixed-effects model with zero-mean deviations.
- Consensus logits are simply team-specific means across bookmakers:

$$\widehat{\text{logit}(p_i)} = \frac{1}{26} \sum_{b=1}^{26} \text{logit}(p_{i,b}).$$

- Consensus winning probabilities are obtained by transforming back to the probability scale:

$$\hat{p}_i = \text{logit}^{-1} \left(\widehat{\text{logit}(p_i)} \right).$$

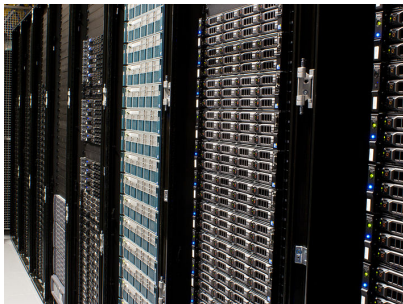
- Model captures 98.7% of the variance in $\text{logit}(p_{i,b})$ and the associated estimated standard error is 0.184.

Modeling consensus and agreement

Team	FIFA code	Probability	Log-odds	Log-ability	Group
Brazil	BRA	16.6	-1.617	-1.778	E
Germany	GER	15.8	-1.673	-1.801	F
Spain	ESP	12.5	-1.942	-1.925	B
France	FRA	12.1	-1.987	-1.917	C
Argentina	ARG	8.4	-2.389	-2.088	D
Belgium	BEL	7.3	-2.546	-2.203	G
England	ENG	4.9	-2.957	-2.381	G
Portugal	POR	3.4	-3.353	-2.486	B
Uruguay	URU	2.7	-3.566	-2.566	A
Croatia	CRO	2.5	-3.648	-2.546	D
		⋮			

Abilities and tournament simulations

$$\Pr(i \text{ beats } j) = \pi_{ij}$$
$$= \frac{\text{ability}_i}{\text{ability}_i + \text{ability}_j}$$



```
tournament.R
~dev/projects/baR/Projects/Euro-2016

Open Save

sim_log_abilities <- function(logodds, groups,
  start = NULL, n = 100000, rounds = 5,
  loss = function(x, y) mean(abs(x - y)), na.rm = TRUE),
  tol = 0.1, maxiter = 100, eps = 1, rate = 0.8,
  cores = NULL, trace = TRUE)
{
  ## main input: winning log-odds
  stopifnot(!is.null(names(logodds)))
  nam <- names(logodds)
  target <- logodds
  if(is.null(start)) start <- logodds
  if(is.null(names(start))) names(start) <- nam

  ## group list
  if(is.null(names(groups))) {
    names(groups) <- nam
  } else {
    groups <- groups[nam]
  }
  groups <- tapply(groups, groups, names)

  ## simulate a full tournament run
  sim1 <- function(log_abilities) {
    simulate_tournament(n = n, probs = get_probs_abilities(exp(log_abilities)),
      groups = groups, cores = cores, rounds = rounds)
  }

  iter <- 1
  if(trace) cat("Start:", start, "\n")
  x <- list()
  y <- list()
  loss_value <- list()
  x[[1]] <- start[names(target)]
  repeat {
    result <- sim1(x[[iter]])
    winner_i <- factor(sapply(result, "[", "winner"), levels = nam)
    prob_i <- pmax(prop.table(table(winner_i)), 1/n)
    y[[iter]] <- qlogis(prob_i)[names(target)]
    if(trace) {
      cat("** Iteration:", iter, "\n")
      cat("** Log_abilities:", x[[iter]], "\n")
    }
    loss_value[[iter]] <- loss(y[[iter]], target)
    if(trace) cat("Value of the loss function:", round(loss_value[[iter]], 4), "\n")
    if((loss_value[[iter]] < tol) || (iter >= maxiter))
      break
    iter <- iter + 1
    x[[iter]] <- x[[iter-1]] - (y[[iter-1]] - target) / abs(y[[iter-1]] - target) * eps / (
  }
  list(log_abilities = x, result = result, loss_value = loss_value)
}
```

Abilities and tournament simulations

Further questions:

- What are the likely courses of the tournament that lead to these bookmaker consensus winning probabilities?
- Is the team with the highest probability also the strongest team?
- What are the winning probabilities for all possible matches?

Motivation:

- Tournament draw might favor some teams.
- Tournament schedule was known to bookmakers and hence factored into their quoted odds.
- Can abilities (or strengths) of the teams be obtained, adjusting for such tournament effects?

Abilities and tournament simulations

Answer: Yes, an approximate solution can be found by simulation when

- adopting a standard model for paired comparisons (i.e., matches),
- assuming that the abilities do not change over the tournament.

Model: Bradley-Terry model for winning/losing in a paired comparison of team i and team j .

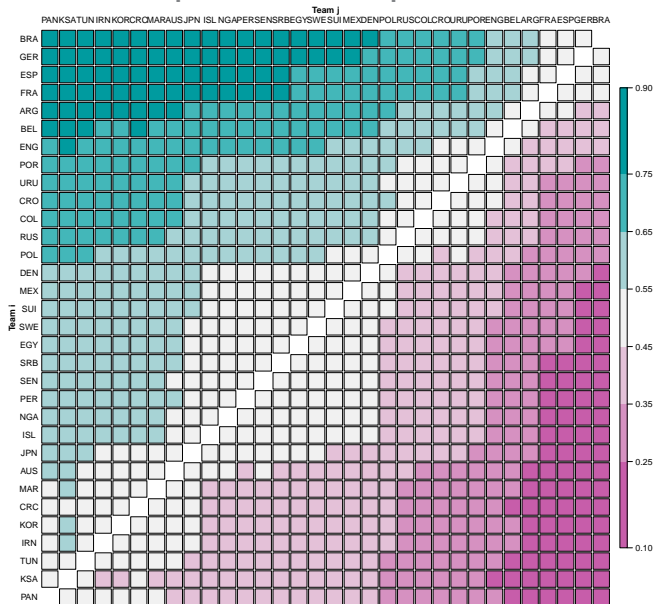
$$\Pr(i \text{ beats } j) = \pi_{i,j} = \frac{ability_i}{ability_i + ability_j}.$$

Abilities and tournament simulations

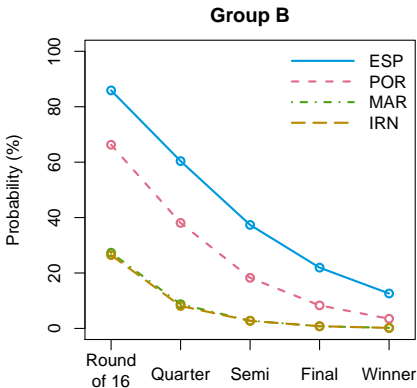
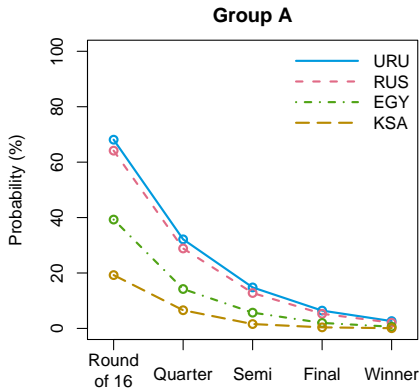
“Reverse” simulation:

- If the team-specific *ability*_{*i*} were known, pairwise probabilities $\pi_{i,j}$ could be computed.
- Given $\pi_{i,j}$ the whole tournament can be simulated (assuming abilities do not change and ignoring possible draws during the group stage).
- Using “many” simulations (here: 1,000,000) of the tournament, the empirical relative frequencies \tilde{p}_i of each team *i* winning the tournament can be determined.
- Choose *ability*_{*i*} for $i = 1, \dots, 32$ such that the simulated winning probabilities \tilde{p}_i approximately match the consensus winning probabilities \hat{p}_i .
- Found by simple iterative local search starting from log-odds.

Abilities and paired comparisons

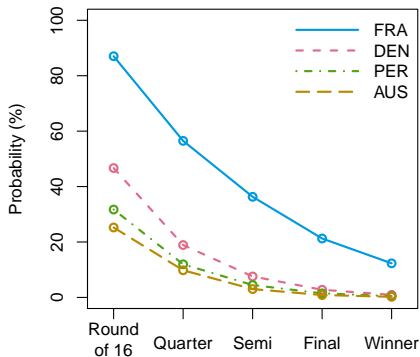


Tournament simulations: Survival curves

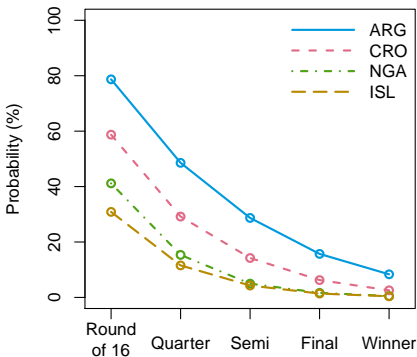


Tournament simulations: Survival curves

Group C

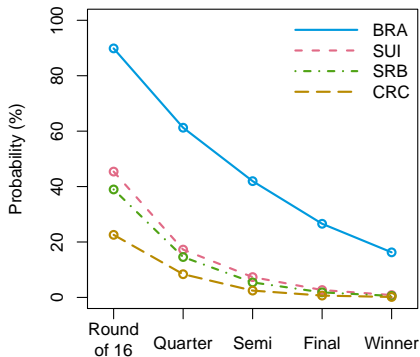


Group D

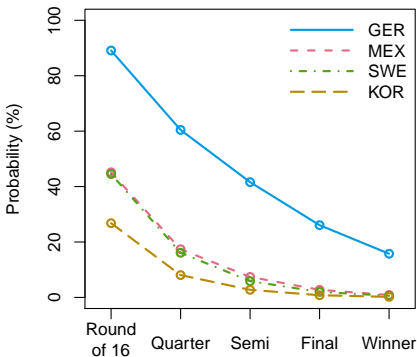


Tournament simulations: Survival curves

Group E

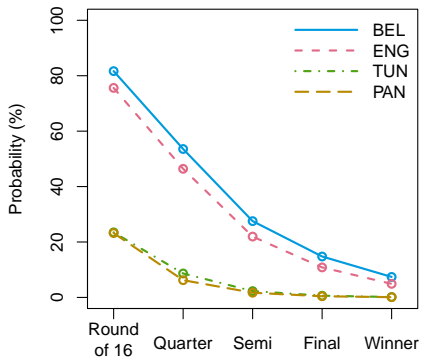


Group F

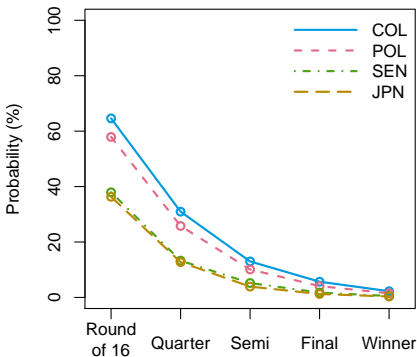


Tournament simulations: Survival curves

Group G



Group H



Outcome verification



Source: Spiegel.de

Outcome verification

Question: Was the bookmaker consensus model any good?

- Ex post the final France vs. Croatia seems very surprising.
- However, especially Croatia profited from Germany and Spain dropping out of the tournament early on.
- Also, Croatia did not win any of the knockout stage games in normal time.

Problems:

- Just a single observation of the tournament and at most one observation of each paired comparison.
- Hard to distinguish between an unlikely outcome and systematic errors in the predicted (prob)abilities.

Outcome verification

Possible approaches:

- Compare forecasts with the observed tournament ranking (1 FRA, 2 CRO, 3 BEL, 4 ENG, 6.5 URU, 6.5 BRA, ...).
- Benchmark against Elo and FIFA ratings.
- Note that the Elo rating also implies ability scores based on which pairwise probabilities and “forward” simulation of tournament can be computed:

$$ability_{Elo,i} = 10^{Elo_i/400}.$$

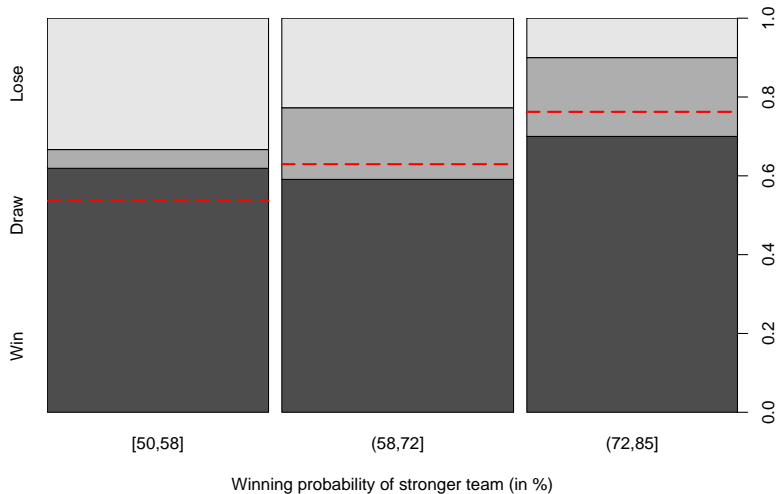
- Check whether pairwise probabilities roughly match empirical proportions from clusters of matches.

Outcome verification: Ranking

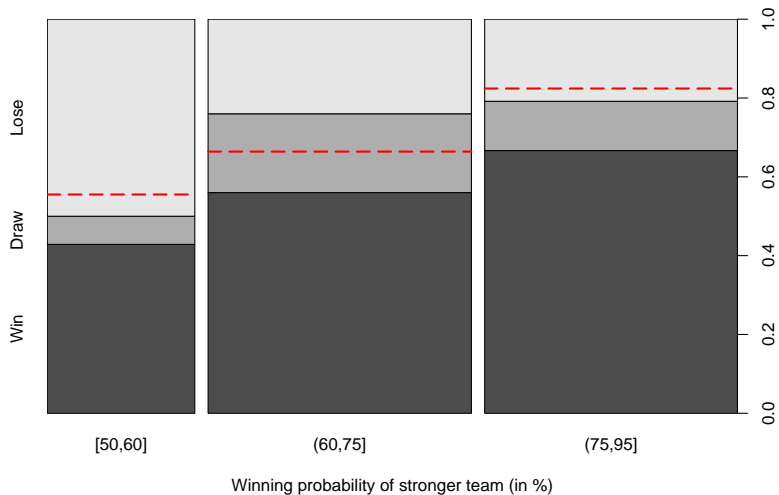
Spearman rank correlation of observed tournament ranking with bookmaker consensus model (BCM) as well as FIFA and Elo ranking:

BCM (Probabilities)	0.704
BCM (Abilities)	0.710
Elo (Probabilities)	0.594
Elo	0.592
FIFA	0.411

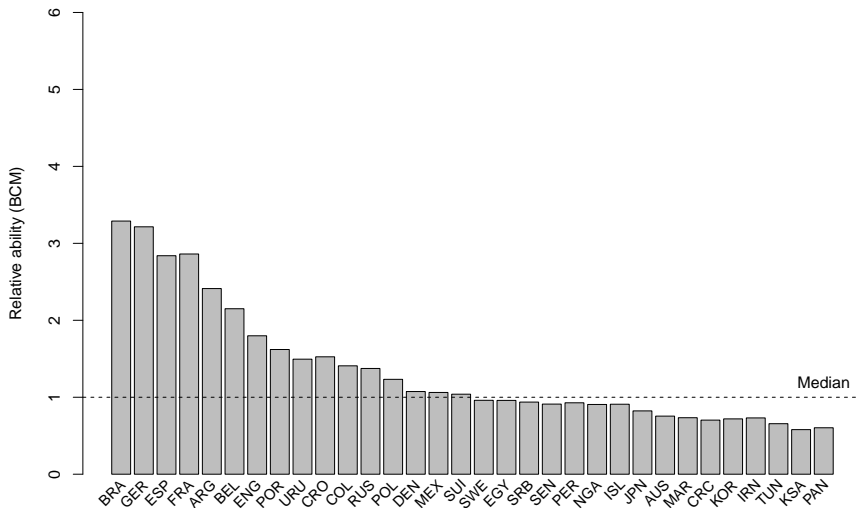
Outcome verification: BCM pairwise prob.



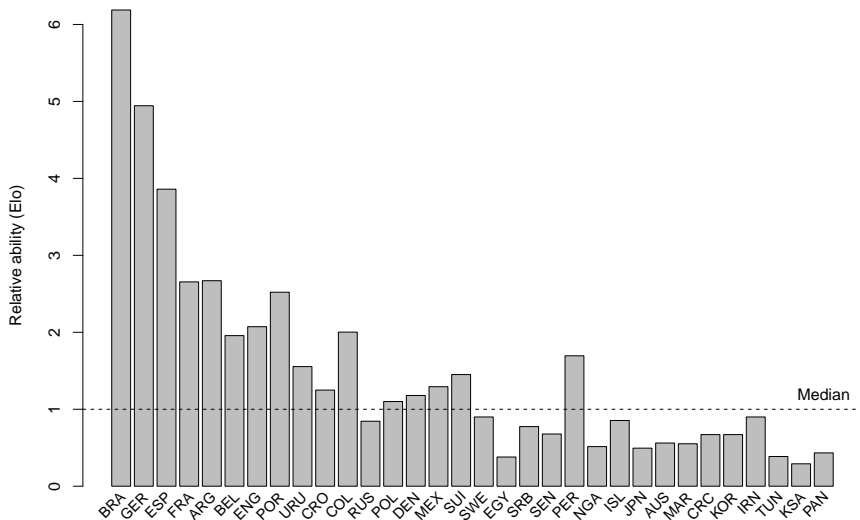
Outcome verification: Elo pairwise prob.



Outcome verification: BCM abilities



Outcome verification: Elo abilities



Discussion

Summary:

- Expert judgments of bookmakers are a useful information source for probabilistic forecasts of sports tournaments.
- Winning probabilities are obtained by adjustment for overround and averaging on log-odds scale.
- Competitor abilities can be inferred by post-processing based on pairwise-comparison model with “reverse” tournament simulations.
- Approach outperformed Elo and FIFA ratings for recent UEFA Euros and FIFA World Cups.

Limitations:

- Matches are only assessed in terms of winning/losing, i.e., no goals, draws, or even more details.
- Inherent chance is substantial and hard to verify.

References

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Leitner C, Zeileis A, Hornik K (2010). "Forecasting Sports Tournaments by Ratings of (Prob)abilities: A Comparison for the EURO 2008." *International Journal of Forecasting*, **26**(3), 471–481.
doi:10.1016/j.ijforecast.2009.10.001.

Groups A and B

Rank	Team	Probability (in %)
1	URU	68.1
2	RUS	64.2
3	KSA	19.2
4	EGY	39.3

Rank	Team	Probability (in %)
1	ESP	85.9
2	POR	66.3
3	IRN	26.5
4	MAR	27.3

Groups C and D

Rank	Team	Probability (in %)
1	FRA	87.0
2	DEN	46.7
3	PER	31.7
4	AUS	25.2

Rank	Team	Probability (in %)
1	CRO	58.7
2	ARG	78.7
3	NGA	41.2
4	ISL	30.9

Groups E and F

Rank	Team	Probability (in %)
1	BRA	89.9
2	SUI	45.4
3	SRB	39.0
4	CRC	22.6

Rank	Team	Probability (in %)
1	SWE	44.5
2	MEX	45.2
3	KOR	26.8
4	GER	89.1

Groups G and H

Rank	Team	Probability (in %)
1	BEL	81.7
2	ENG	75.6
3	TUN	23.5
4	PAN	23.2

Rank	Team	Probability (in %)
1	COL	64.6
2	JPN	36.3
3	SEN	37.9
4	POL	57.9